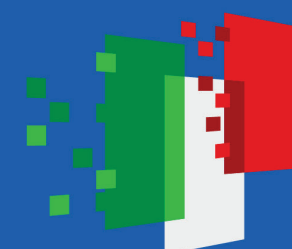




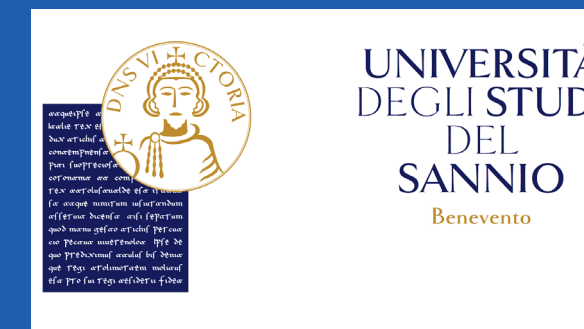
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Free-Most Project

BANDO PUBBLICO PER LA SELEZIONE DI PROPOSTE PROGETTUALI, FINALIZZATE ALLA CONCESSIONE DI FINANZIAMENTI PER ATTIVITÀ COERENTI CON GLI OBIETTIVI DEL CENTRO NAZIONALE PER LA MOBILITÀ SOSTENIBILE, A VALERE SULLE RISORSE DEL PIANO NAZIONALE RIPRESA E RESILIENZA (PNRR) MISSIONE 4, “ISTRUZIONE E RICERCA” - COMPONENTE 2, “DALLA RICERCA ALL’IMPRESA” - LINEA DI INVESTIMENTO 1.4 “CENTRI NAZIONALI”, FINANZIATO DALL’UNIONE EUROPEA – NEXTGENERATIONEU” PROGETTO CNMS – Centro Nazionale Mobilità Sostenibile – Codice Identificativo CN00000023, SPOKE 12 – SUSTAINABLE PROPULSION – CUP B43C22000440001

Presenter: Davide Liuzza (University of Sannio)

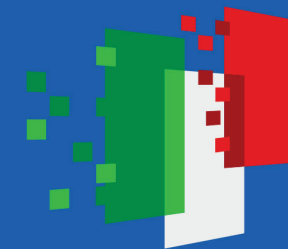
June 19th, 2025



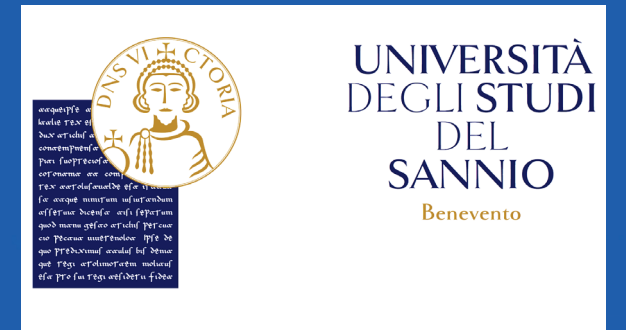
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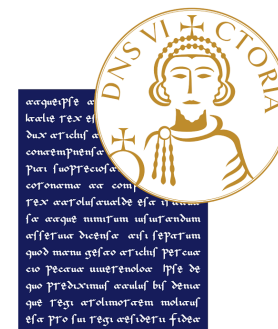


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Project overview

- Name: **Free-Most**
- Duration: **10 months** (started on August 2024)
- Budget: **270.000 €**
- Partners:
 - **University of Sannio**
 - **CNR – STEMS**
 - **Vanvitelli University**



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Luigi Vanvitelli



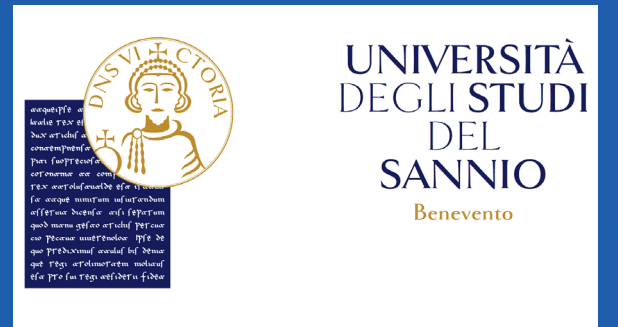
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Project aim in brief

- Modeling study of free piston linear generator (FPLG) system with a specific focus on the electromagnetic part jointly with power converter and a battery
- Control system study and design for a FPLG coupled with battery
- Digital twin development for the system FPLG + power converter + battery
- Magnetic design of a FPLG
- Desing and setup of an experimental test rig for a FPLG system



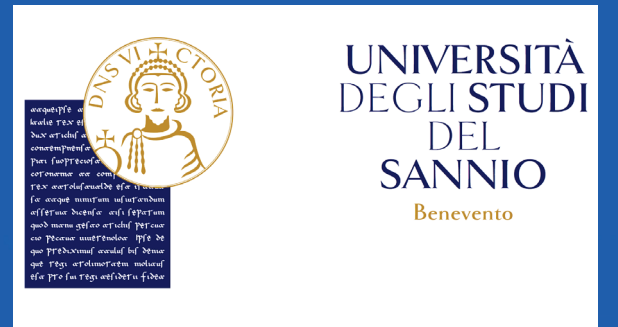
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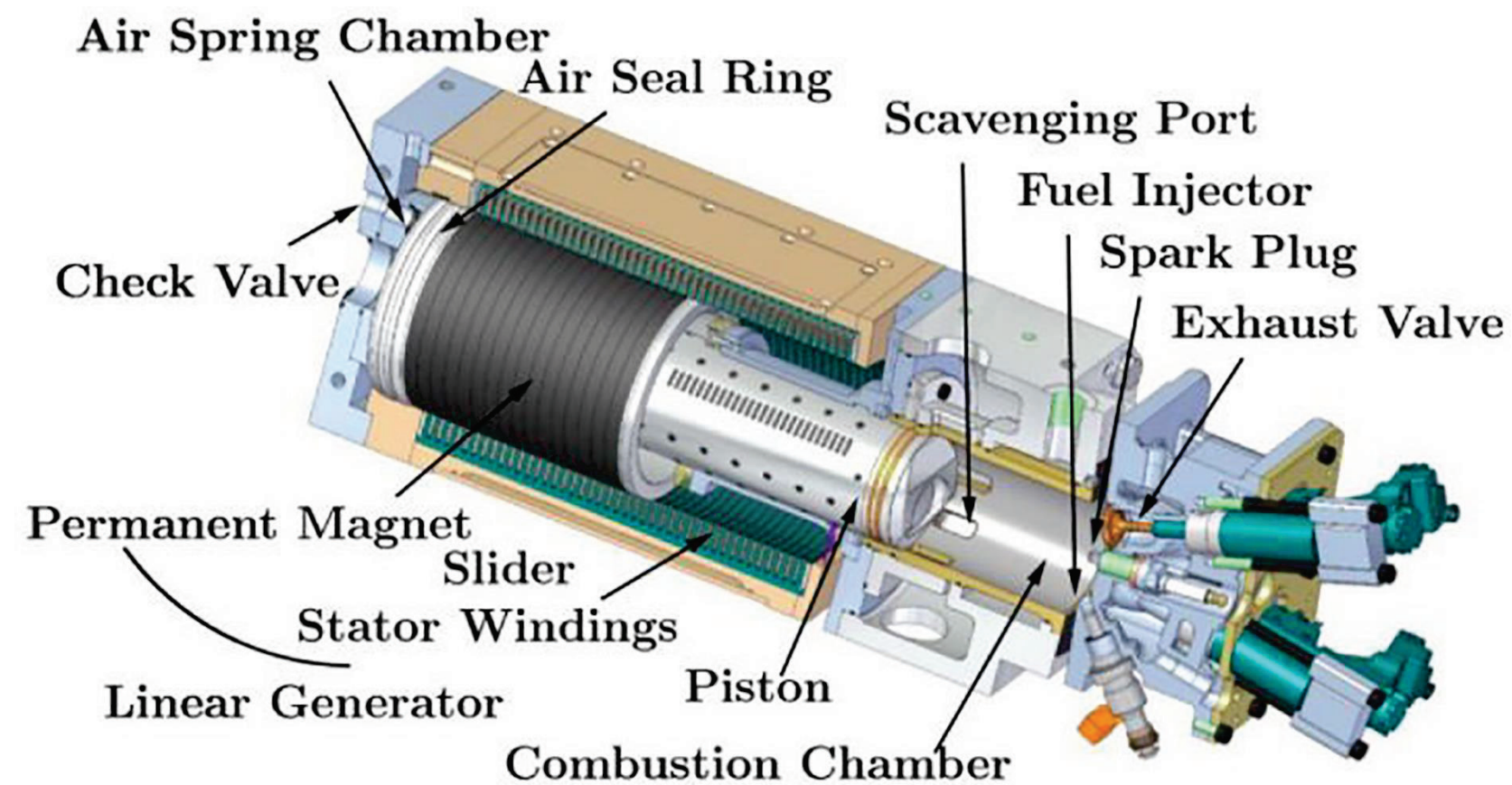
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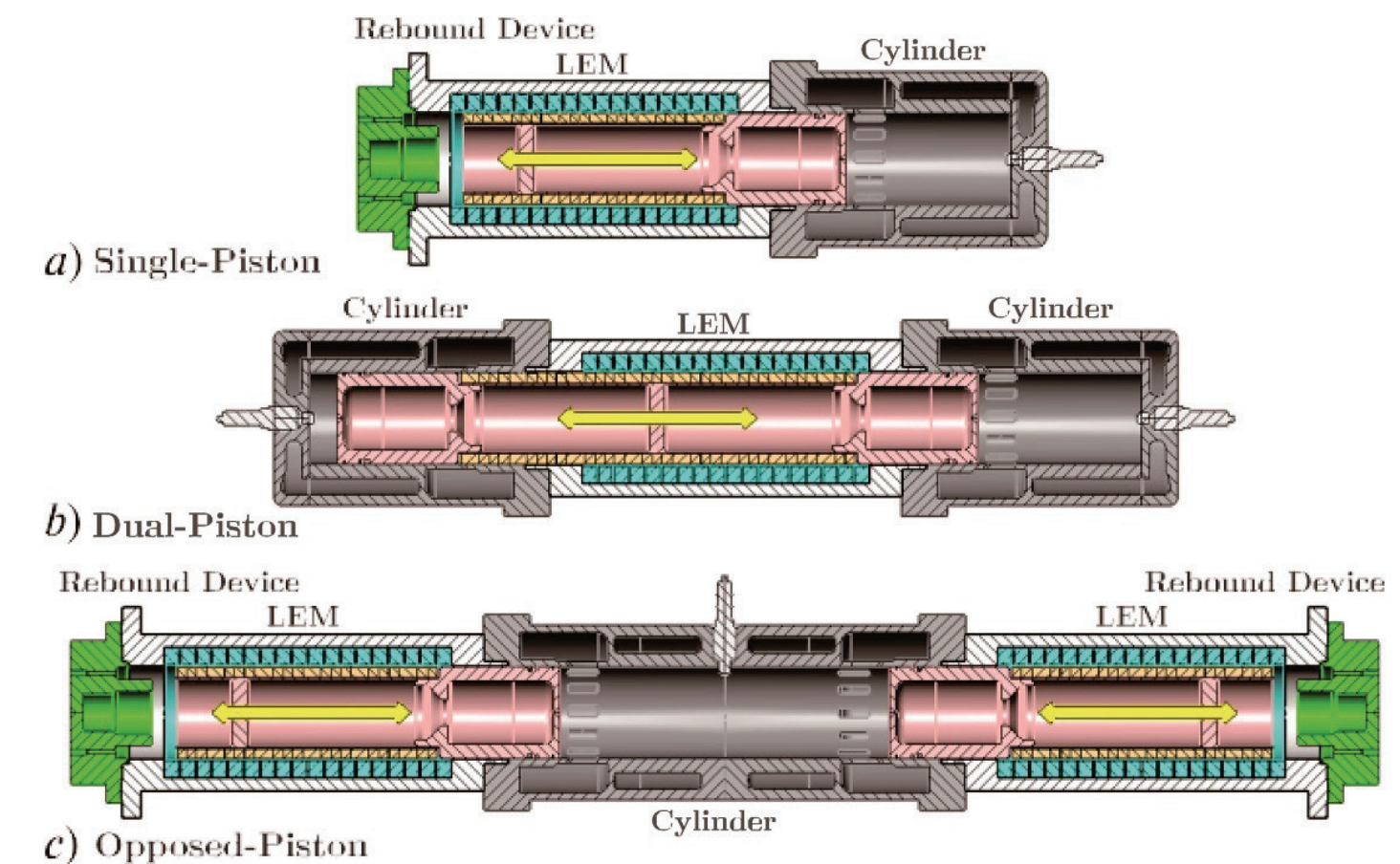


What is a FPLG?



A Toyota gas FPLG

- Main components:
 - Combustion chamber(s)
 - Linear electric motor/generator (permanent magnets on the mover)
 - Rebound chamber
- Main configurations





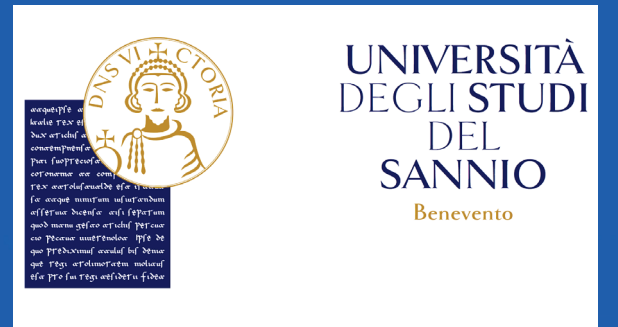
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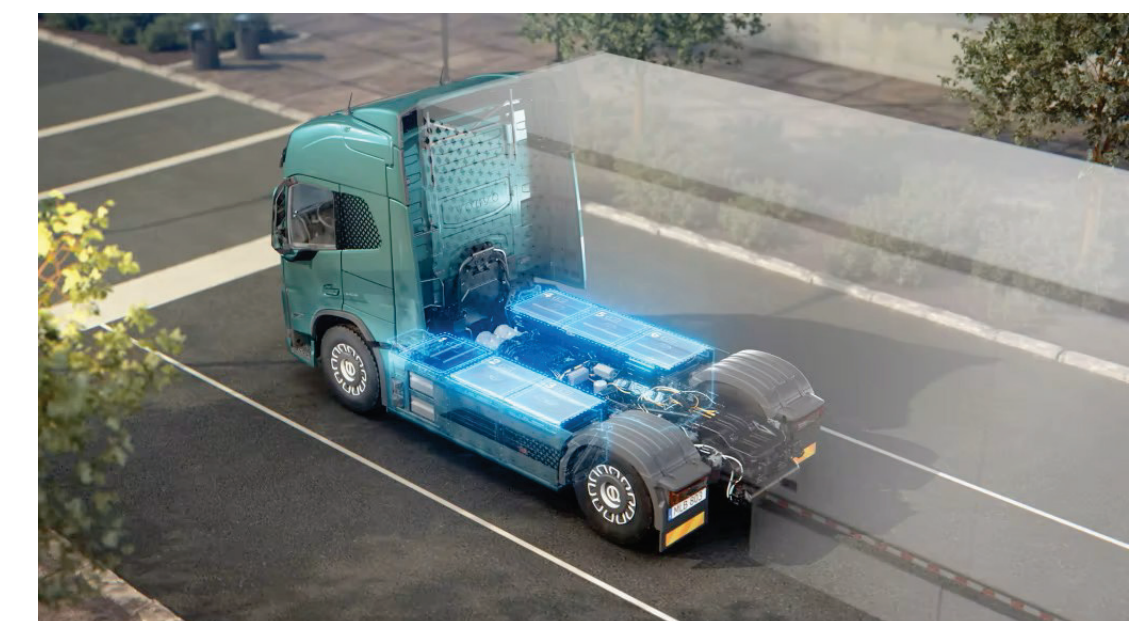
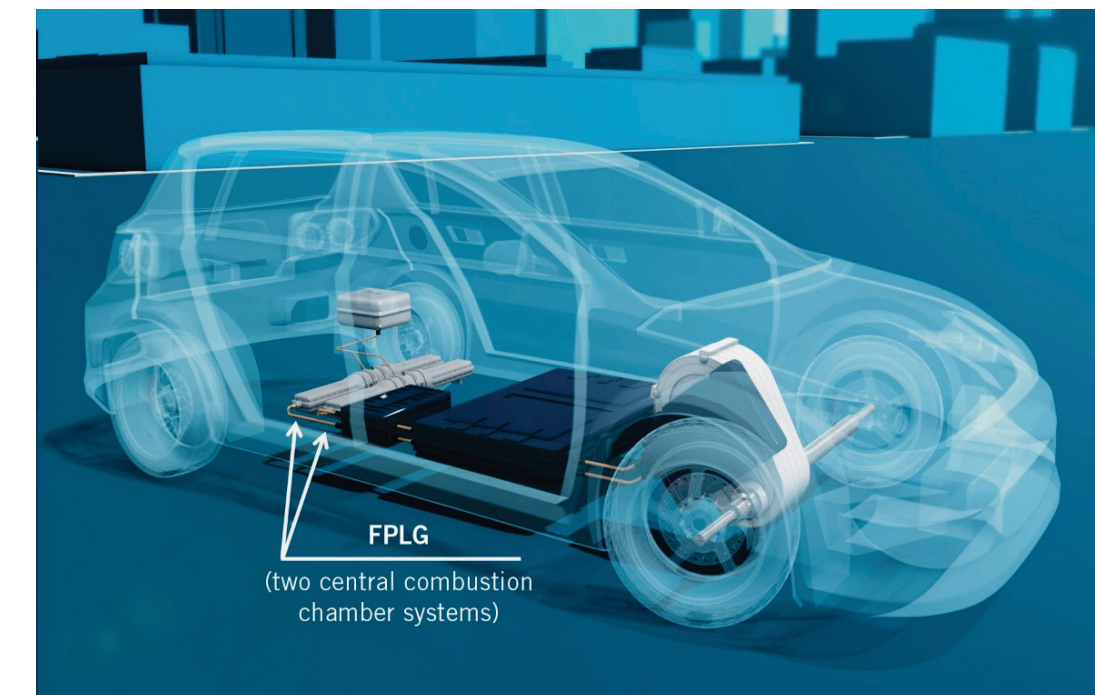


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Motivation

- The EU has clearly set its sights on battery electric mobility
- Large sectors of transportation (especially heavy vehicles, work machinery and shipping) are ill-suited for battery storage-based traction
- Battery-powered cars are not experiencing the expected market growth:
 - Insufficient recharging infrastructure
 - higher costs compared to traditional traction (both vehicles and recharges)
- Battery based solutions do not guarantee, at the moment, EU independence from battery producers, especially China

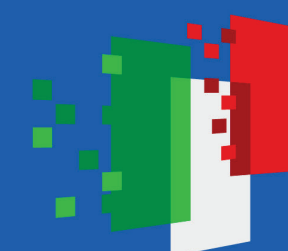




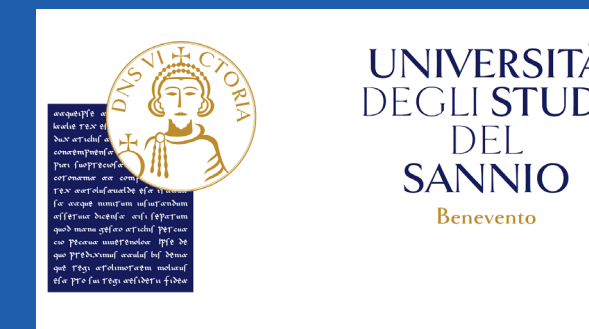
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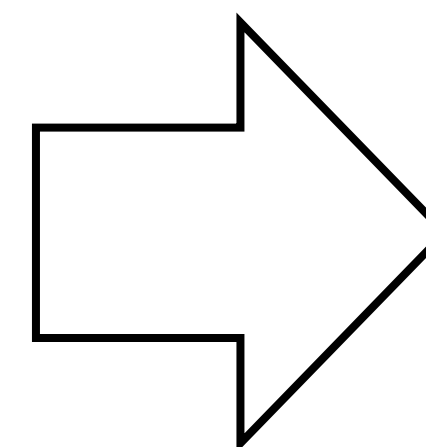


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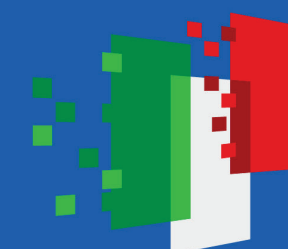
- Need for technical solutions for large transportation sectors
- Need for economically feasible transitions solution (CO₂ reduction despite immature infrastructure)
- Need for strategic alternatives



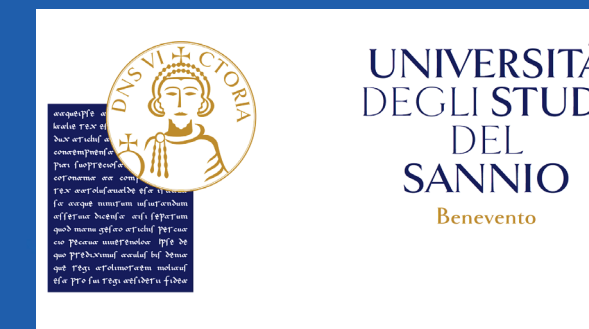
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Advantages of FPLG solutions

Automotive

- FPLGs represent a potential alternative for range-extender automotive solutions
 - Less vibrations and noise due to the absence of crankshaft
 - Higher potential efficiency due to reduced friction forces
 - Adaptable combustion chamber
 - Multi-fuel
- High potential in the Italian automotive market (a green transition acceptable by consumers) allowing for high production values:
 - Italian engineering industry invoices about 400 billions € (8% of GDP)
 - Italian engineering industry accounts for more than half of Italy's exports

Other sectors

- Due to its compact size, FPLG can be also envisioned for:
 - Uninterrupted/Emergency power systems
 - Auxiliary power units for aircrafts, ships and large vehicles
 - Residential co-generation units



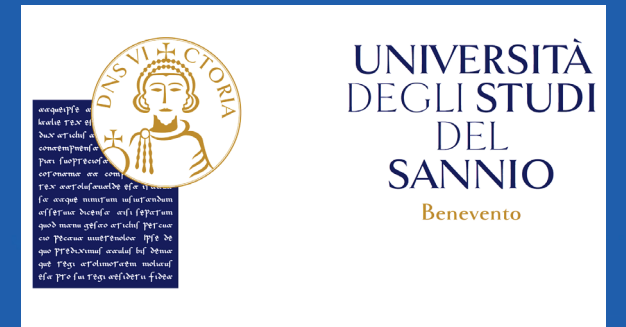
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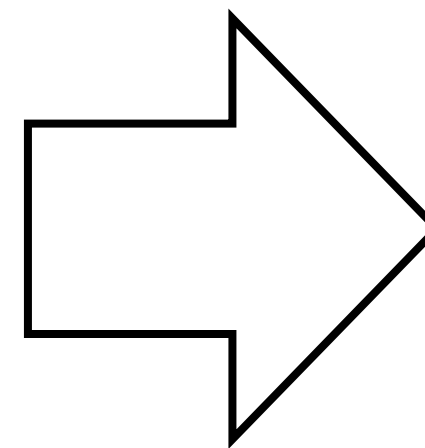


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Challenges of FPLG

- Difficult to control the FPLG motion/generation due to non-constant velocities of the piston
- Difficult to integrate battery and converter models with the FPLG model
- Difficult to handle fluctuating currents for battery recharging
- Lack of sufficient theoretical and experimental studies for specific range extender applications



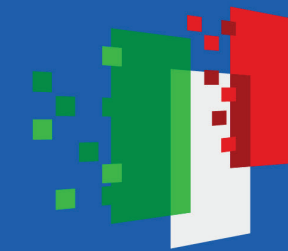
- As said, the Free-Most projects aims to address these issues



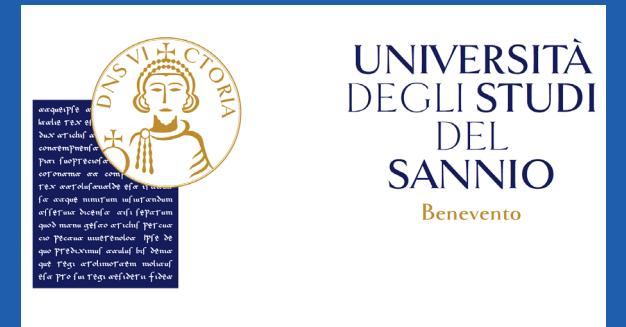
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Modeling - overview

- The modeling has been conducted under some constructive assumptions:
 - Opposed piston with perfectly symmetric forces, i.e., reduced to the single piston case
 - Ideal gas assumption
 - Lumped parameters, uniform temperature and gas pressure
 - Three-phase motor
 - Only self inductance is considered for each coil



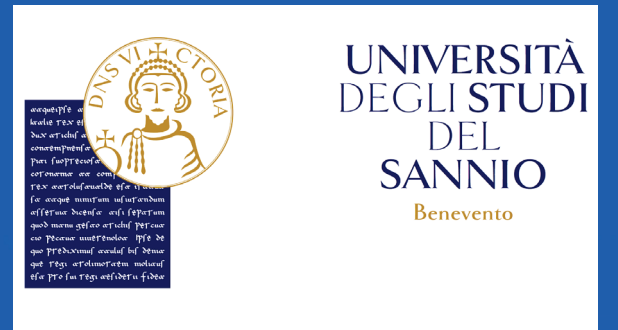
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Modeling - scheme

Mechanical model

$$m \frac{dv}{dt} = A_c p_c - A_r p_r + F_e(z, i_{rst}) - F_f(p_c, v) - F_f(p_r, v)$$

$$\frac{dz}{dt} = v$$

z, v, i_{rst}

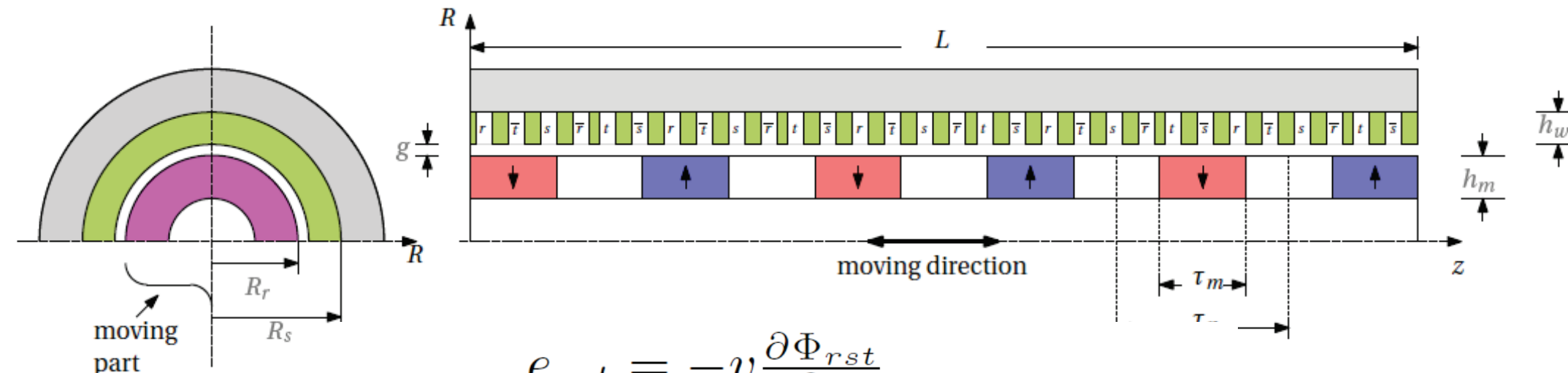
p_c, z, v

i_{rst}, e_{rst}

Thermodynamical model

$$\frac{dp_c}{dt} = \frac{\gamma - 1}{A_c z + V_0} \left(\dot{Q}_c - \dot{Q}_{ht}(p_c, z) \right) - \frac{p_c \gamma}{m_{air}} \frac{dm_{air}}{dt} - \frac{A_c p_c \gamma}{A_c z + V_0} v$$

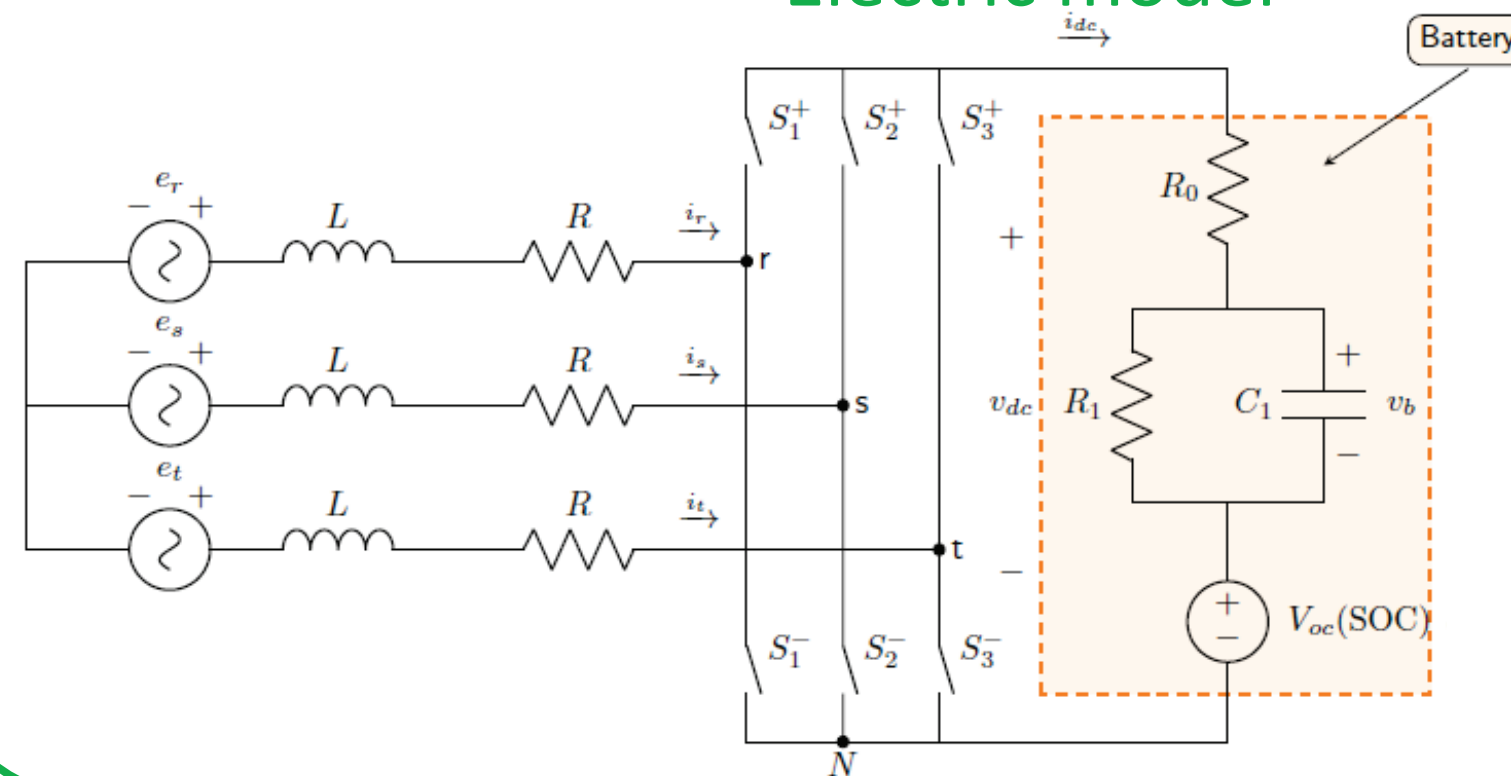
Magnetic model



$$e_{rst} = -v \frac{\partial \Phi_{rst}}{\partial z}$$

$$F_e(z, i_{rst}) = \frac{1}{v} e_{rst}^T i_{rst} = -\frac{\partial \Phi_{rst}^T}{\partial z} i_{rst}$$

Electric model



$$L \frac{di_{\alpha\beta}}{dt} = -R i_{\alpha\beta} + e_{\alpha\beta} - \sigma_{\alpha\beta} v_{dc}$$

$$C_1 \frac{dv_b}{dt} = -\frac{1}{R_1} v_b + i_{dc}$$

$$\frac{dSoC}{dt} = \frac{1}{Q} i_{dc}$$

$$\sigma_{\alpha\beta}^T i_{\alpha\beta} = \frac{2}{3} \sigma_{rst}^T i_{rst} = \frac{2}{3} i_{dc}$$

- z, v position, velocity
- p_c chamber pressure
- i_{rst} currents
- e_{rst} voltages
- Φ_{rst} magnetic flows
- σ_{rst} switch signals
- i_{dc} battery current
- SoC state of charge

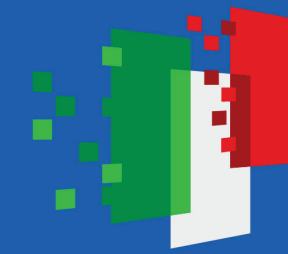
❖ S. Baccari, C. Beatrice, C. Capasso,, O. Veneri, "Integration of free piston linear generator and battery pack in hybrid vehicles", ESARS-ITEC 2024



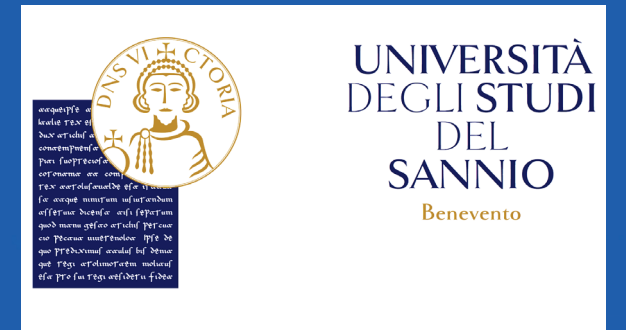
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Control – assumptions

- For the three phase model a control has been derived
- This control is meant for the project envisioned test rig:
 - The piston is moved according to a mover which emulates the combustion expansion and rebound (or any periodic movement)
 - The current generation is controlled so as to recharge a battery
- Fast switching (averaging) assumption:
 - Signals of the switches are continuous in the interval $[0,1]$



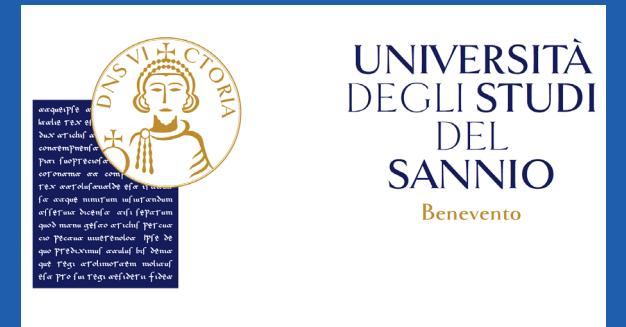
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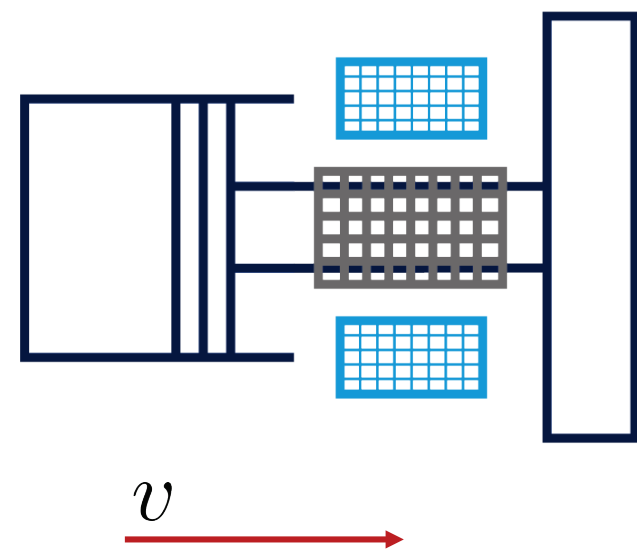


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Control – piston movement

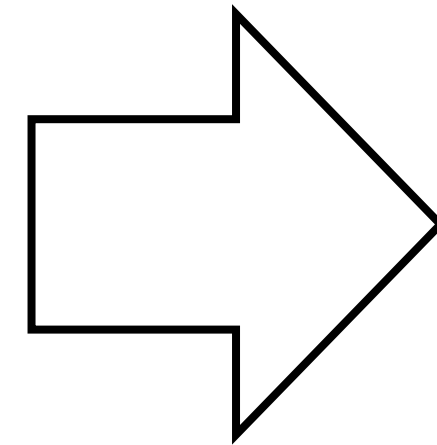
- We consider a harmonic movement of the piston to design the controller



$$v = V \cos \theta_m$$

$$\theta_m = \omega_m t, \omega_m = 2\pi/T_m$$

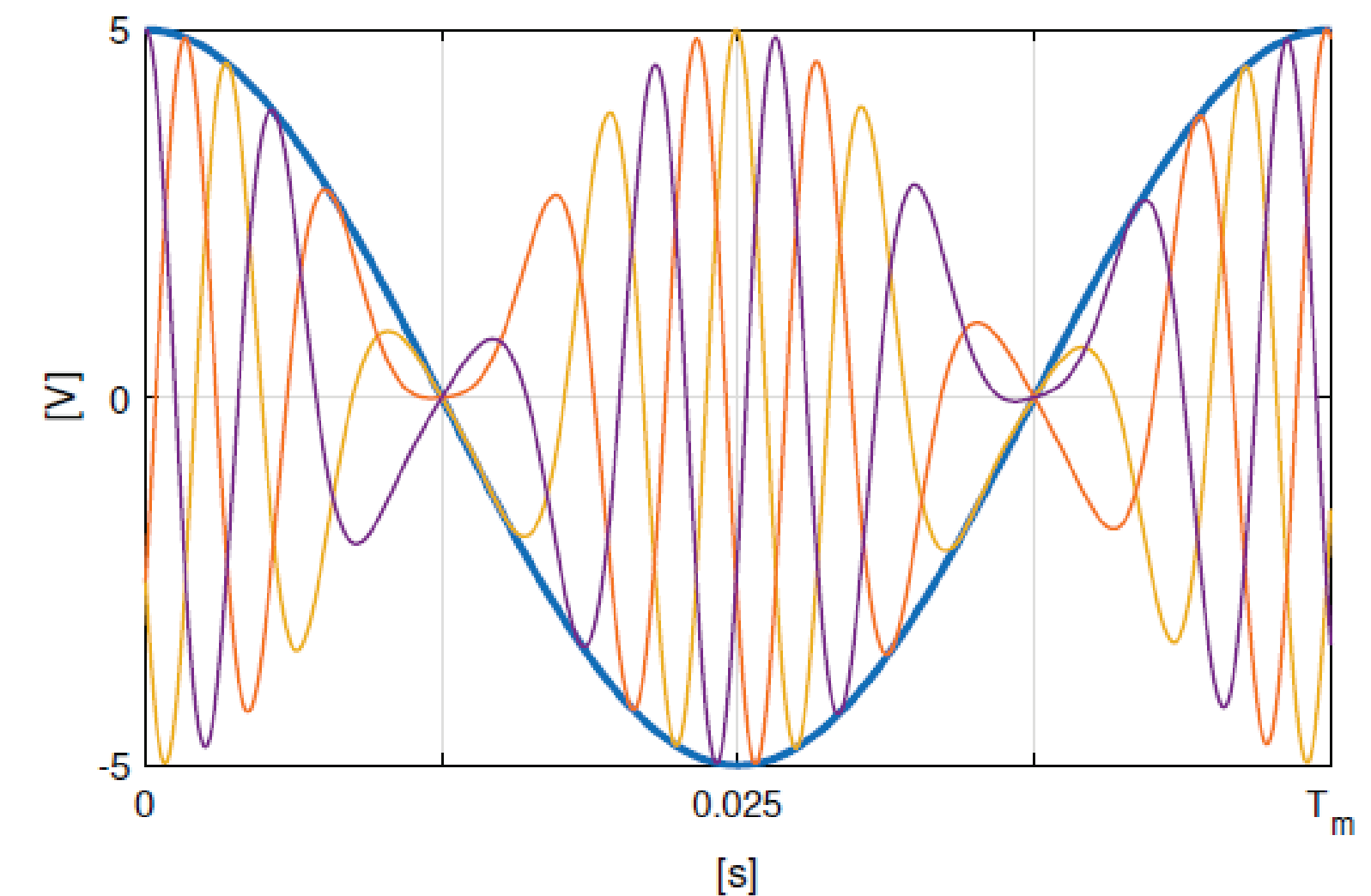
complete trip (forward-
backward) period



$$e_{rst} = \varphi v \begin{pmatrix} \cos \theta \\ \cos(\theta - \frac{2\pi}{3}) \\ \cos(\theta - \frac{4\pi}{3}) \end{pmatrix}$$

$$\frac{d\theta}{dt} = \frac{\hat{\mu}}{V} \omega_m |v| = \mu \omega_m |v|$$

← electrical phase



Time evolution of v and normalized
voltages e_{rst}/φ



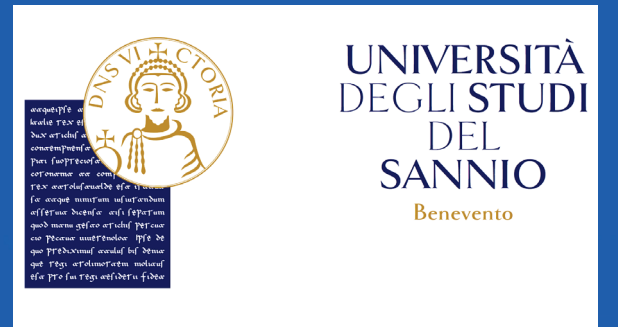
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Control – Clarke transformation and notch filter

- Three phase

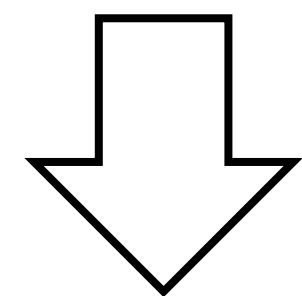
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$$L \frac{dx_t}{dt} = -Rx_t + e_t - e_r + L \frac{dx_r}{dt} + Rx_r - (q_t - q_r)e_b$$

- Switches

$$q_j = \begin{cases} 1 & \text{if } S_j^+ \text{ is on and } S_j^- \text{ is off} \\ 0 & \text{otherwise} \end{cases}$$



Clarke transformation

$$L \frac{di_{\alpha\beta}}{dt} = -Ri_{\alpha\beta} + e_{\alpha\beta} - \sigma_{\alpha\beta}e_b$$

$$e_{\alpha\beta} = \varphi v \begin{pmatrix} \cos \theta \\ \sin \theta \end{pmatrix}$$



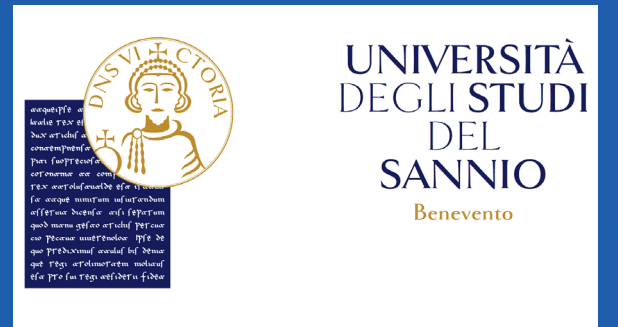
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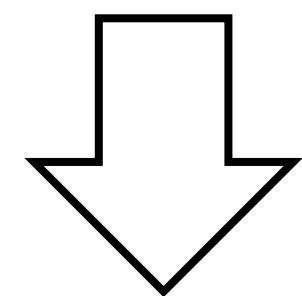
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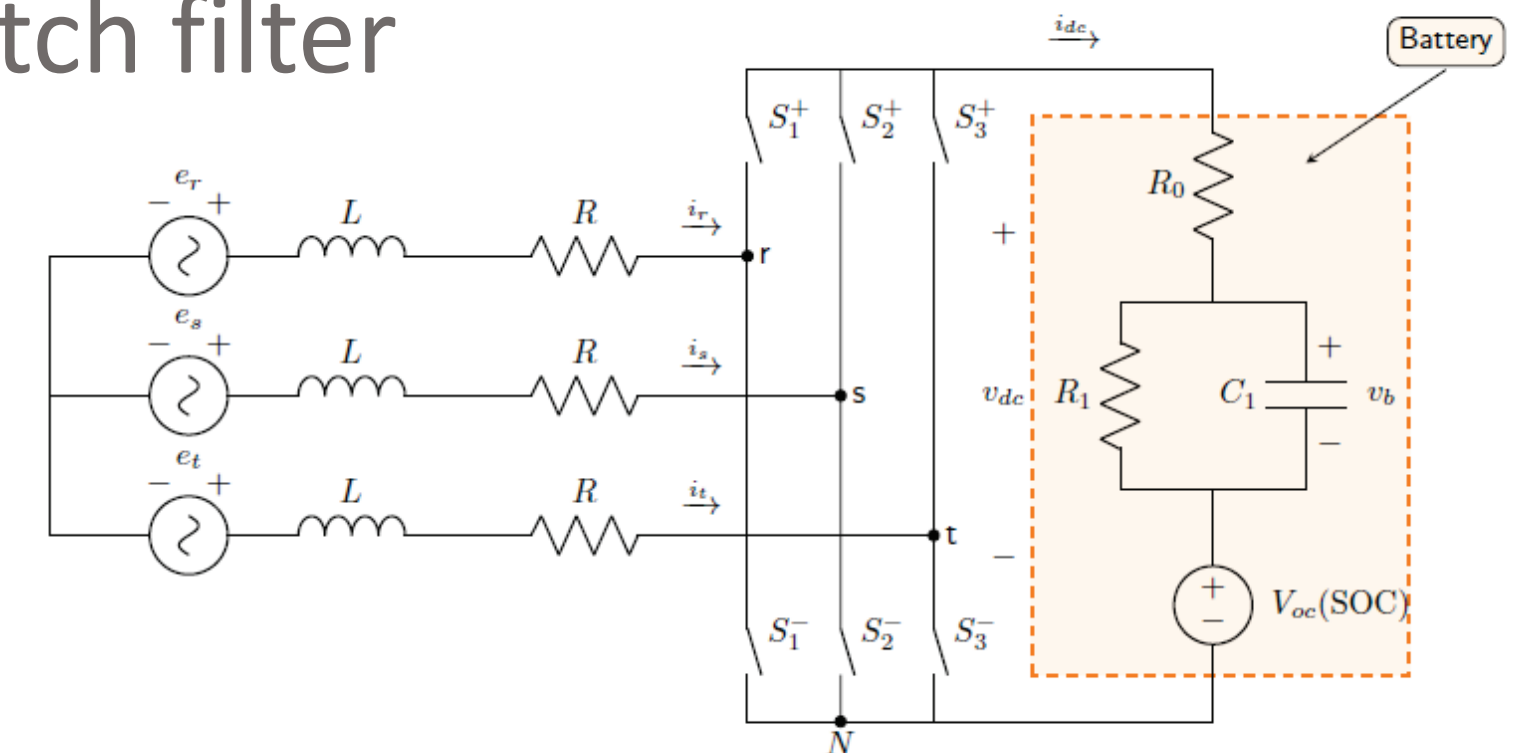
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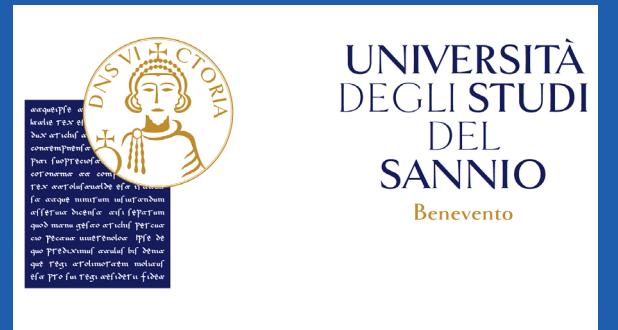
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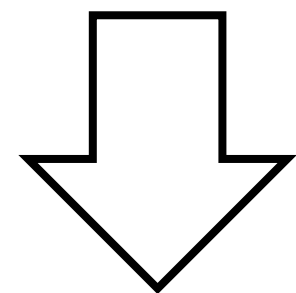
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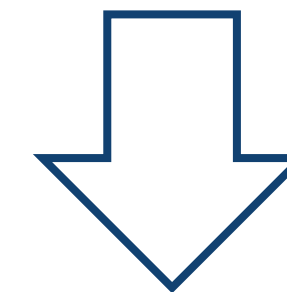
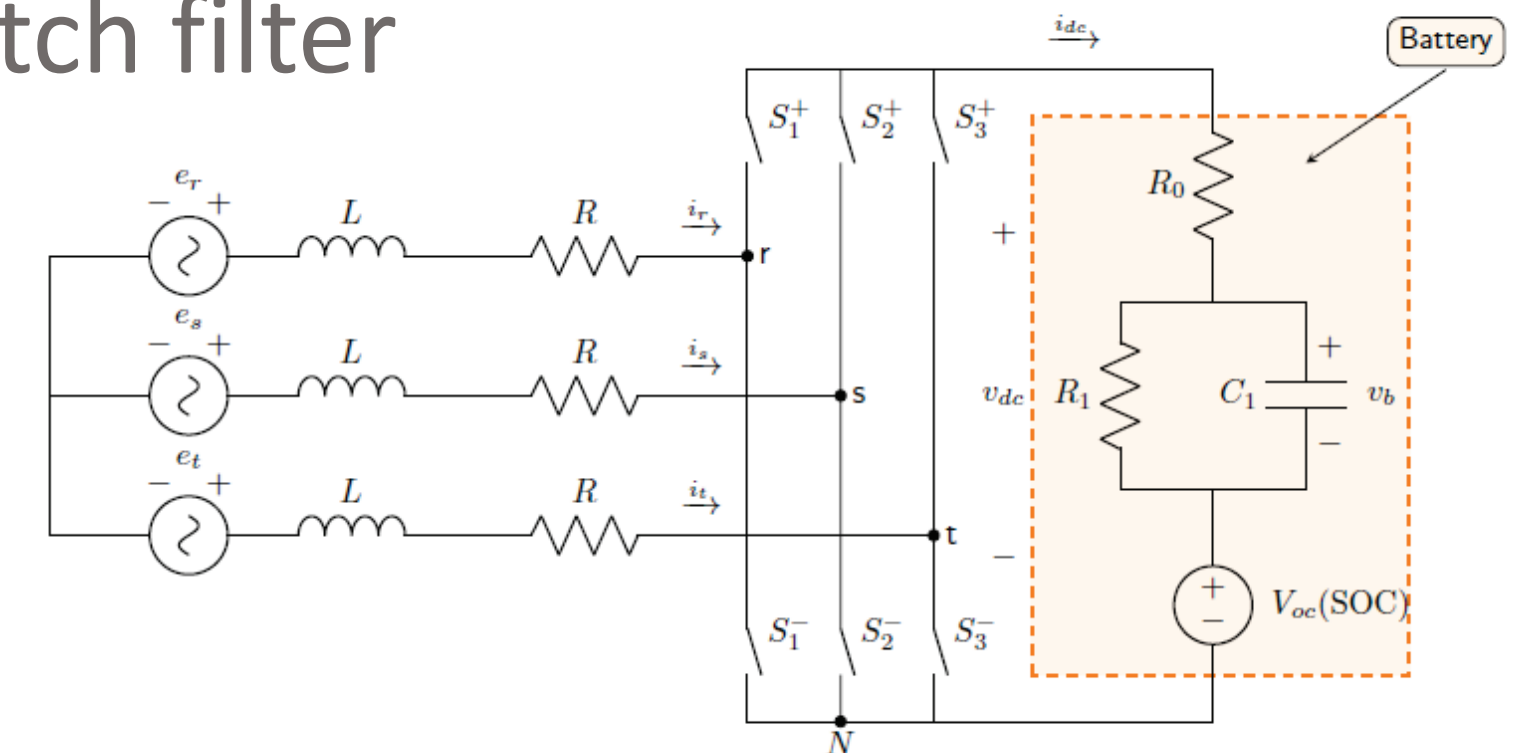
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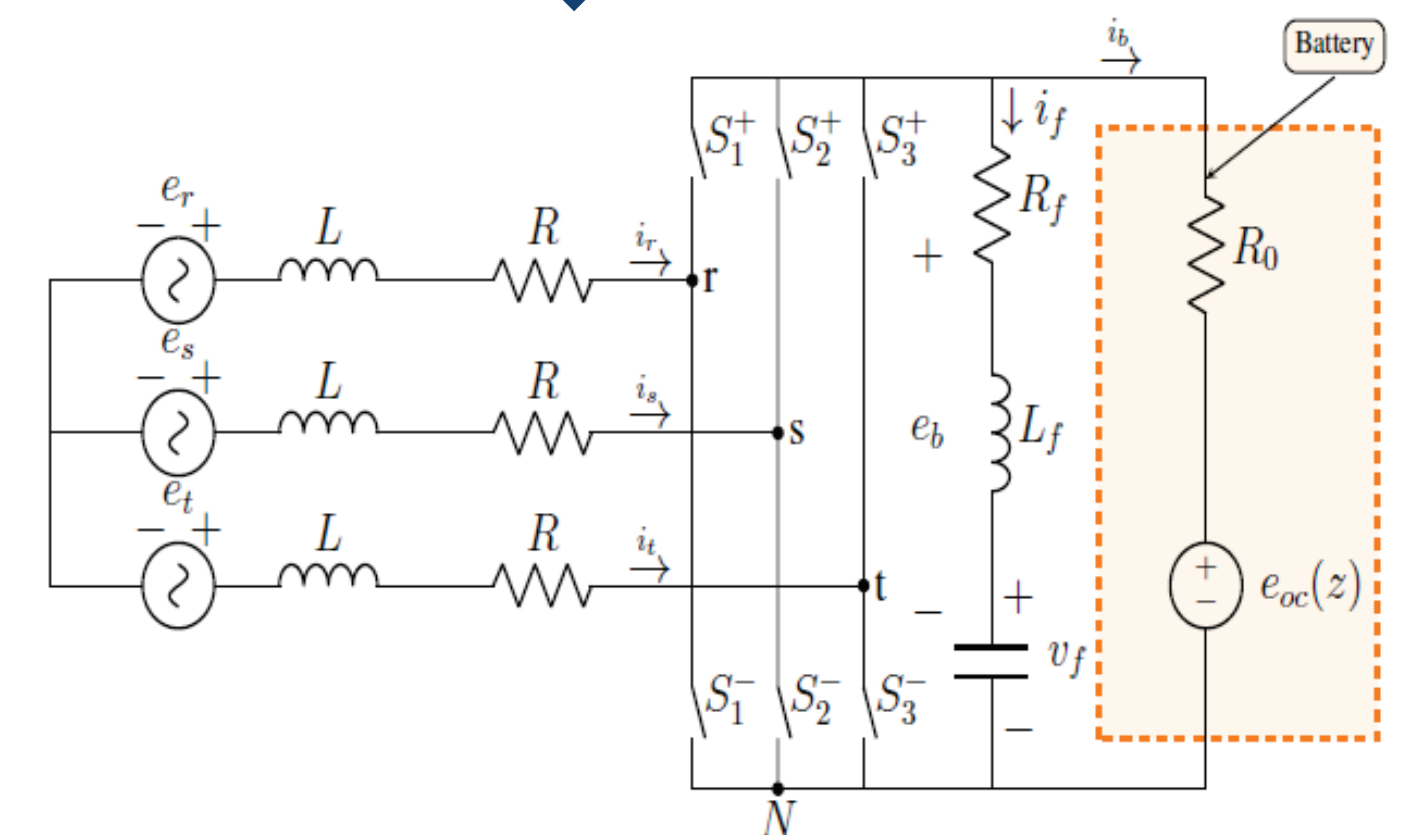
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A notch filter is added





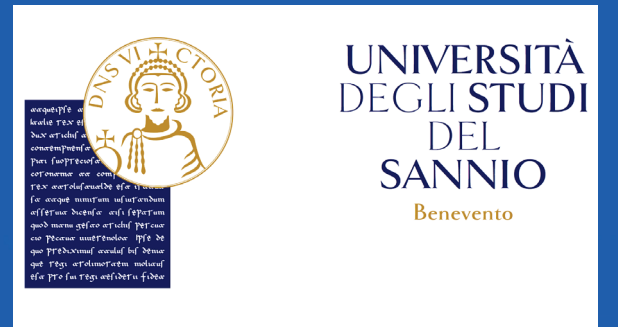
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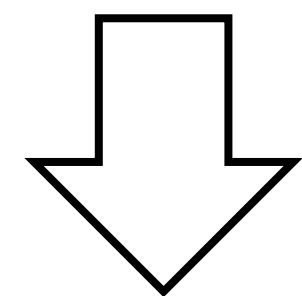
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- Switches

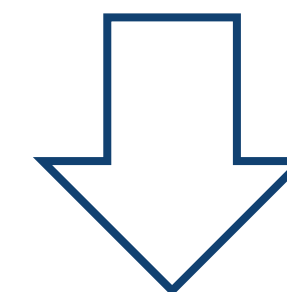
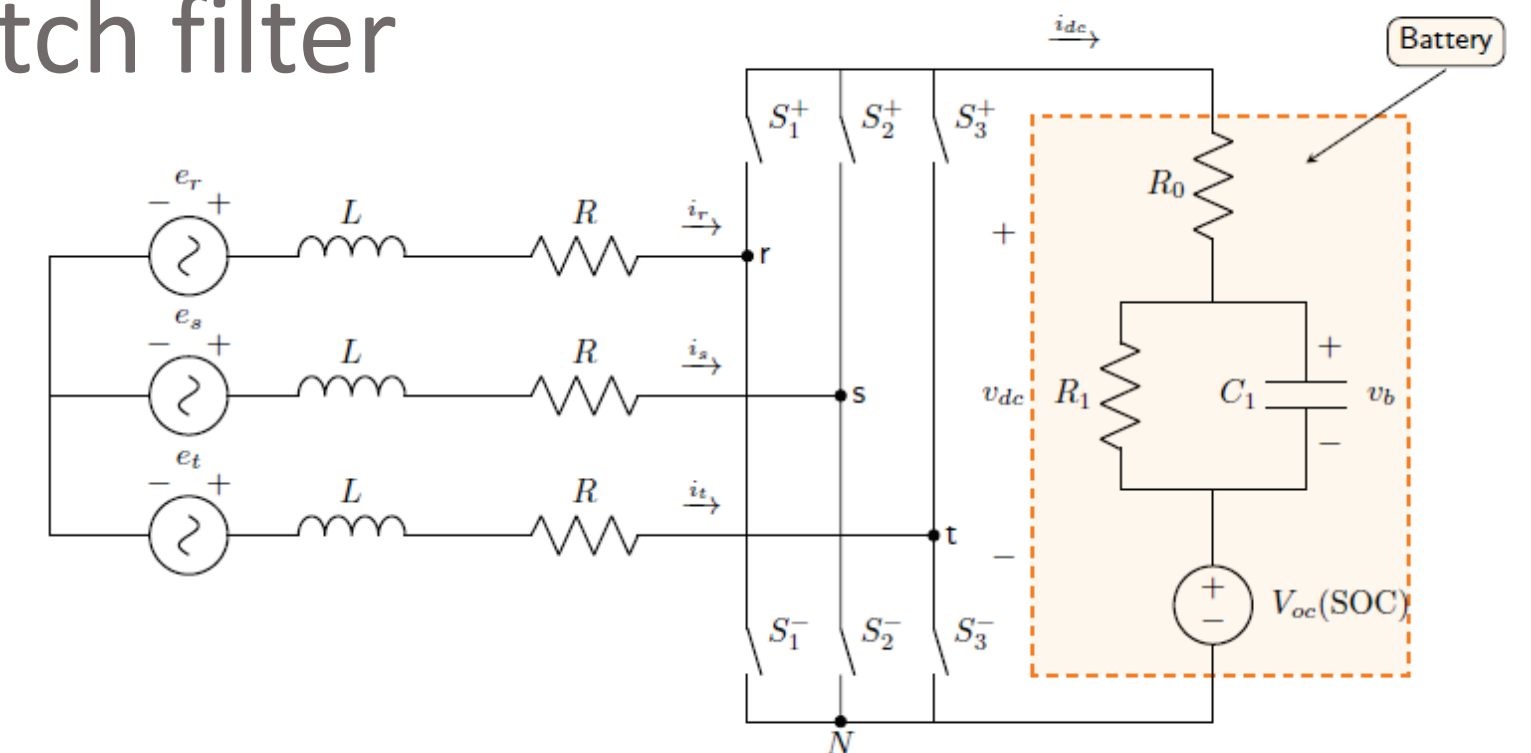
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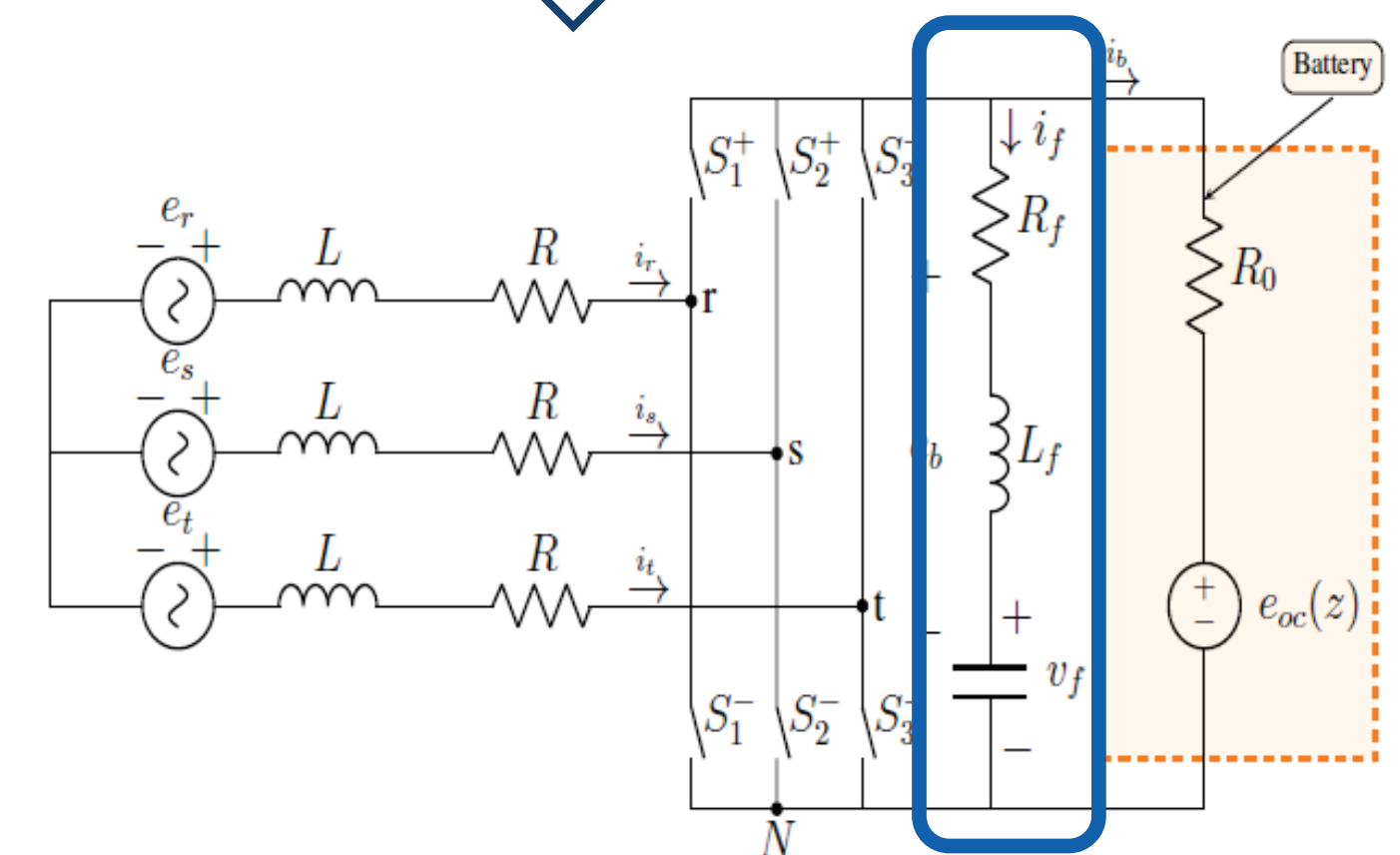
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$$e_{\alpha\beta} = \varphi v \begin{pmatrix} \cos \theta \\ \sin \theta \end{pmatrix}$$



A notch filter is added





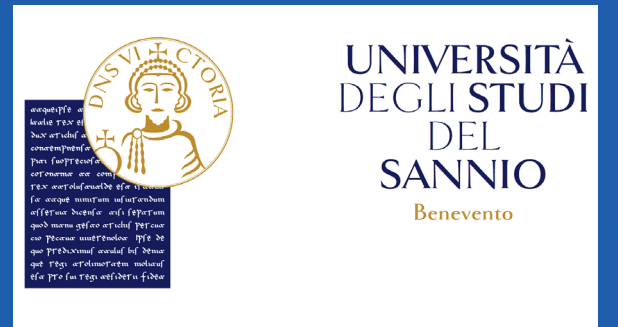
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Control – Filter and battery

- Current from the FPLG

$$\sigma_{\alpha\beta}^T i_{\alpha\beta} = \frac{2}{3} y$$

$$y = i_b + i_f$$

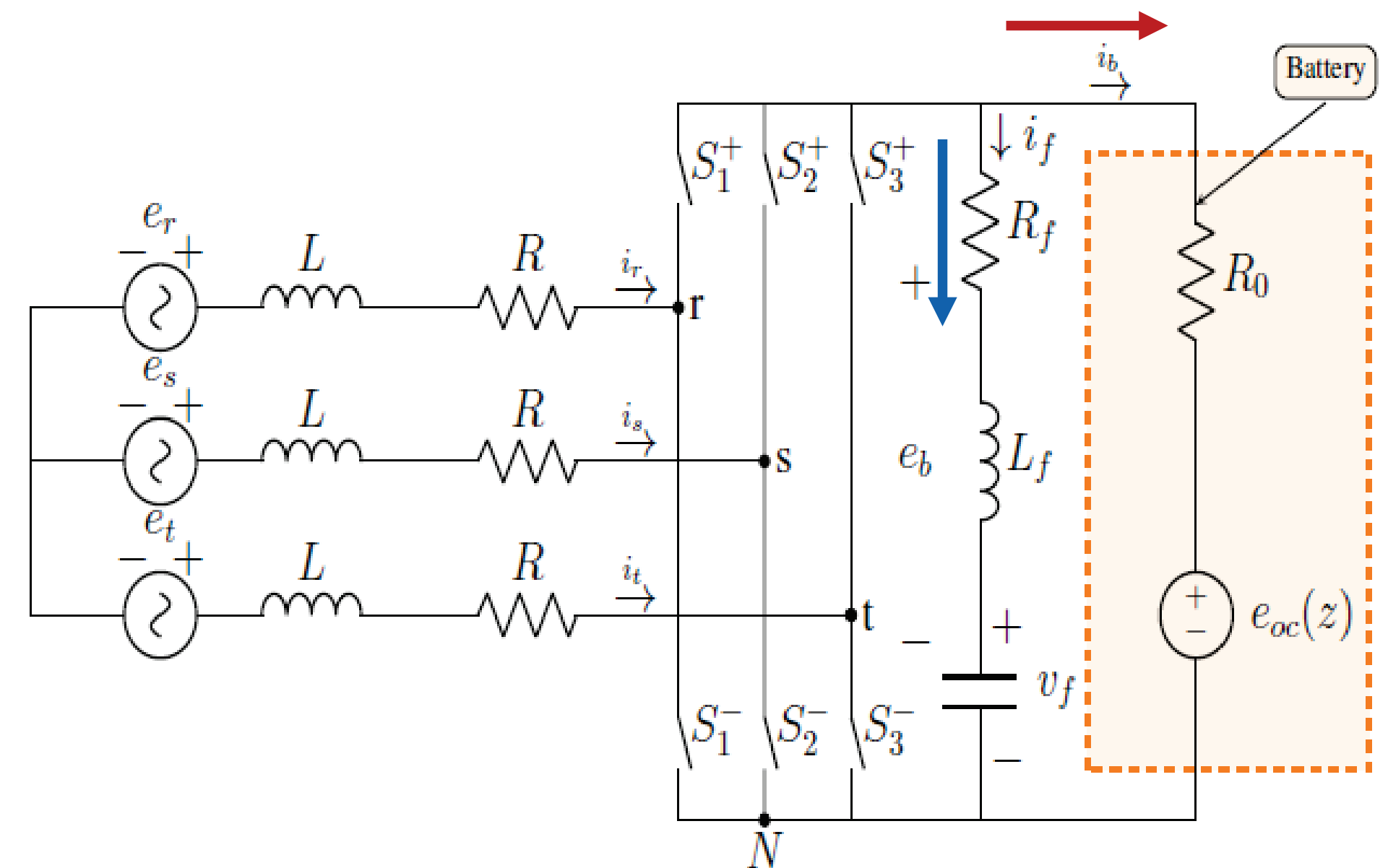
- Filter

$$L_f \frac{di_f}{dt} = -R_f i_f - v_f + e_b$$

$$C_f \frac{dv_f}{dt} = i_f$$

- Battery

$$Q \frac{dz}{dt} = i_b$$

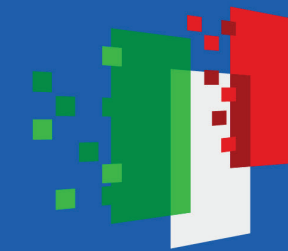




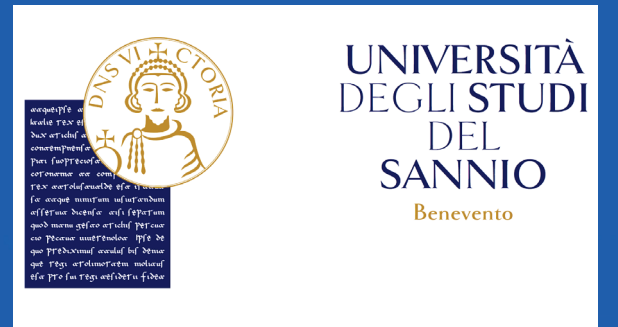
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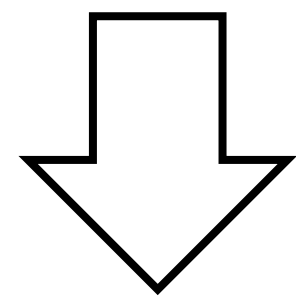


Control – direct/quadrature transformation

$$i_{dq} = \Gamma(\theta) i_{\alpha\beta}$$

$$e_{dq} = \Gamma(\theta) e_{\alpha\beta}$$

$$\Gamma(\theta) = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix}$$



Direct/quadrature
transformation

$$L \frac{di_d}{dt} = -Ri_d + \mu|v|\omega_m Li_q + \varphi v - \sigma_d e_b$$

$$L \frac{di_q}{dt} = -\mu|v|\omega_m Li_d - Ri_q - \sigma_q e_b$$

$$y = \frac{3}{2}(\sigma_d i_d + \sigma_q i_q)$$



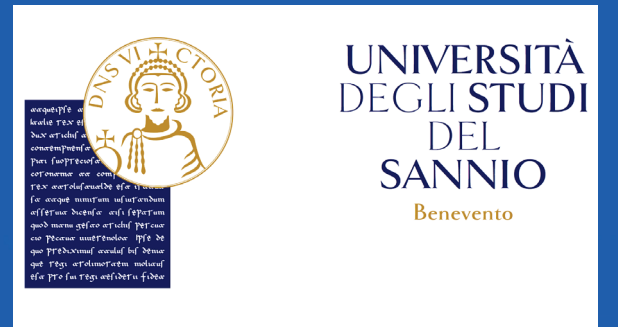
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Control – direct/quadrature transformation

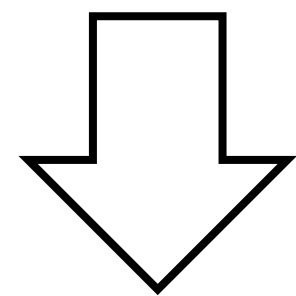
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$$\Gamma(\theta) = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix}$$

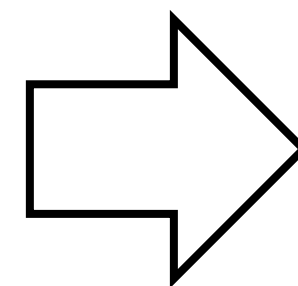
- Quadrature control

$$\sigma_q = -\frac{\mu|v|\omega_m Li_d}{e_b}$$



Direct/quadrature
transformation

σ_q control is designed to
have $i_q = 0$ at steady state



$$L \frac{di_d}{dt} = -Ri_d + \mu|v|\omega_m Li_q + \varphi v - \sigma_d e_b$$

$$L \frac{di_q}{dt} = -\mu|v|\omega_m Li_d - Ri_q - \sigma_q e_b$$

$$y = \frac{3}{2}(\sigma_d i_d + \sigma_q i_q)$$

$$L \frac{di_d}{dt} = -Ri_d + \varphi V \cos \theta_m - \sigma_d e_b$$

$$y = \frac{3}{2}\sigma_d i_d$$



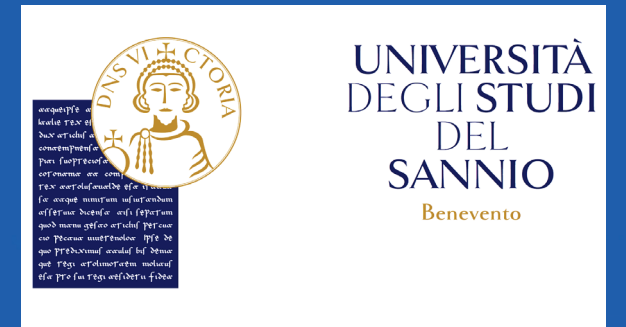
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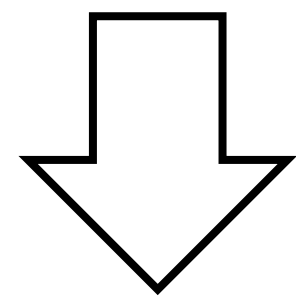


Control – direct/quadrature transformation

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$$e_{dq} = \Gamma(\theta)e_{\alpha\beta}$$

$$\Gamma(\theta) = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix}$$



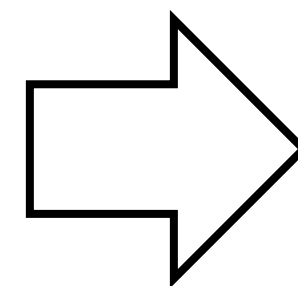
Direct/quadrature
transformation

$$L \frac{di_d}{dt} = -Ri_d + \mu|v|\omega_m Li_q + \varphi v - \sigma_d e_b$$

$$L \frac{di_q}{dt} = -\mu|v|\omega_m Li_d - Ri_q - \sigma_q e_b$$

$$y = \frac{3}{2}(\sigma_d i_d + \sigma_q i_q)$$

σ_q control is designed to
have $i_q = 0$ at steady state

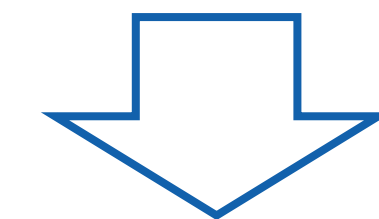


- Quadrature control

$$\sigma_q = -\frac{\mu|v|\omega_m Li_d}{e_b}$$

$$L \frac{di_d}{dt} = -Ri_d + \varphi V \cos \theta_m - \sigma_d e_b$$

$$y = \frac{3}{2} \sigma_d i_d$$



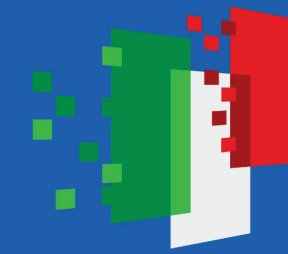
Decomposed as steady state +
sinusoidal solution



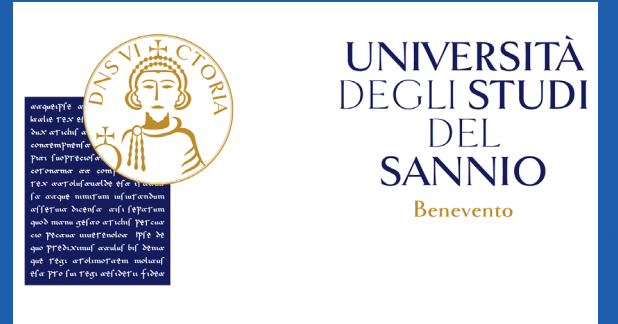
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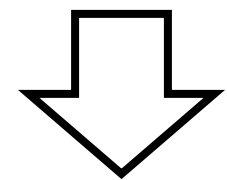


Control – decomposition steady state + sinusoidal

- Sinusoidal solution form

$$i_d = i_{da} \cos \theta_m + i_{db} \sin \theta_m$$

$$\sigma_d = \sigma_{da} \cos \theta_m + \sigma_{db} \sin \theta_m$$



$$\frac{2}{3}y = \frac{\sigma_{da}i_{da} + \sigma_{db}i_{db}}{2} + \frac{\sigma_{da}i_{da} - \sigma_{db}i_{db}}{2} \cos 2\theta_m + \frac{\sigma_{da}i_{db} + \sigma_{db}i_{da}}{2} \sin 2\theta_m$$



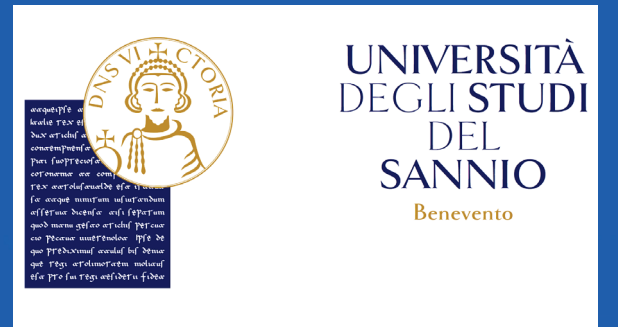
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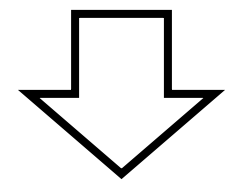


Control – decomposition steady state + sinusoidal

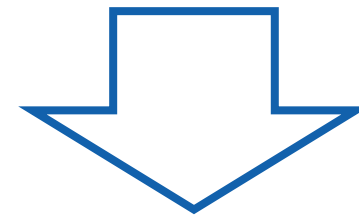
- Sinusoidal solution form

$$i_d = i_{da} \cos \theta_m + i_{db} \sin \theta_m$$

$$\sigma_d = \sigma_{da} \cos \theta_m + \sigma_{db} \sin \theta_m$$



$$\frac{2}{3}y = \frac{\sigma_{da}i_{da} + \sigma_{db}i_{db}}{2} + \frac{\sigma_{da}i_{da} - \sigma_{db}i_{db}}{2} \cos 2\theta_m + \frac{\sigma_{da}i_{db} + \sigma_{db}i_{da}}{2} \sin 2\theta_m$$



Removed by the filter

$$i_b = \frac{3}{4}(\sigma_{da}i_{da} + \sigma_{db}i_{db})$$

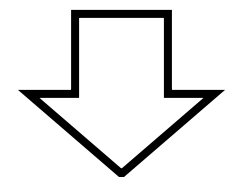


Control – decomposition steady state + sinusoidal

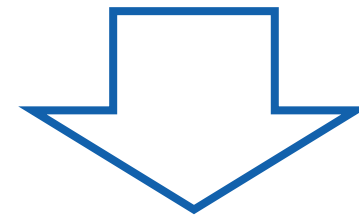
- Sinusoidal solution form

$$i_d = i_{da} \cos \theta_m + i_{db} \sin \theta_m$$

$$\sigma_d = \sigma_{da} \cos \theta_m + \sigma_{db} \sin \theta_m$$

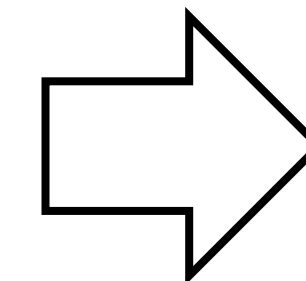


$$\frac{2}{3}y = \frac{\sigma_{da}i_{da} + \sigma_{db}i_{db}}{2} + \frac{\sigma_{da}i_{da} - \sigma_{db}i_{db}}{2} \cos 2\theta_m + \frac{\sigma_{da}i_{db} + \sigma_{db}i_{da}}{2} \sin 2\theta_m$$



Removed by the filter

$$i_b = \frac{3}{4}(\sigma_{da}i_{da} + \sigma_{db}i_{db})$$



- Feedback and feedforward control decomposition

$$\sigma_{da} = \sigma_{da}^{\text{ff}} + \sigma_{da}^{\text{fb}}$$

$$\sigma_{db} = \sigma_{db}^{\text{ff}} + \sigma_{db}^{\text{fb}}$$



Control – decomposition steady state + sinusoidal

- Sinusoidal solution form

$$i_d = i_{da} \cos \theta_m + i_{db} \sin \theta_m$$

$$\sigma_d = \sigma_{da} \cos \theta_m + \sigma_{db} \sin \theta_m$$

$$\frac{2}{3}y = \frac{\sigma_{da}i_{da} + \sigma_{db}i_{db}}{2} + \frac{\sigma_{da}i_{da} - \sigma_{db}i_{db}}{2} \cos 2\theta_m + \frac{\sigma_{da}i_{db} + \sigma_{db}i_{da}}{2} \sin 2\theta_m$$

Removed by the filter

$$i_b = \frac{3}{4}(\sigma_{da}i_{da} + \sigma_{db}i_{db})$$

- Feedback and feedforward control decomposition

$$\sigma_{da} = \sigma_{da}^{\text{ff}} + \sigma_{da}^{\text{fb}}$$

$$\sigma_{db} = \sigma_{db}^{\text{ff}} + \sigma_{db}^{\text{fb}}$$

$$\sigma_{da}^{\text{ff}} = \frac{-Ri_{da}^{\text{ref}} + \varphi V}{e_b}$$

$$\sigma_{db}^{\text{ff}} = -\frac{\omega_m L i_{da}^{\text{ref}}}{e_b}$$

FF is designed to
keep the steady
state solution

$$L \frac{d\hat{i}_{da}}{dt} = -R\hat{i}_{da} + \omega_m L \hat{i}_{db} - \sigma_{da}^{\text{fb}} e_b$$

$$L \frac{d\hat{i}_{db}}{dt} = -\omega_m L \hat{i}_{da} - R\hat{i}_{db} - \sigma_{db}^{\text{fb}} e_b$$

$$u_{da} = \omega_m L \hat{i}_{db} - \sigma_{da}^{\text{fb}} e_b$$

$$u_{db} = -\omega_m L \hat{i}_{da} - \sigma_{db}^{\text{fb}} e_b$$

FB is designed
with feedback
linearization +
PD



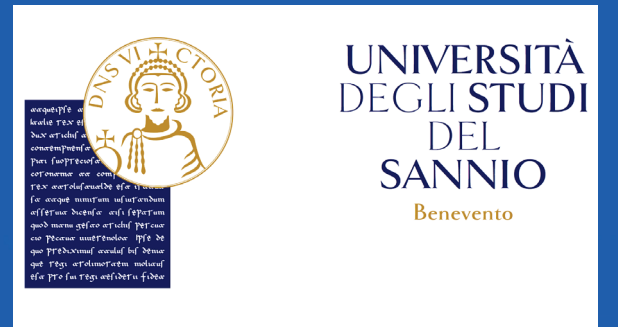
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Control – numerical analysis

- A digital twin of the FLPG + Battery + Control has been developed in Matlab/Simulink



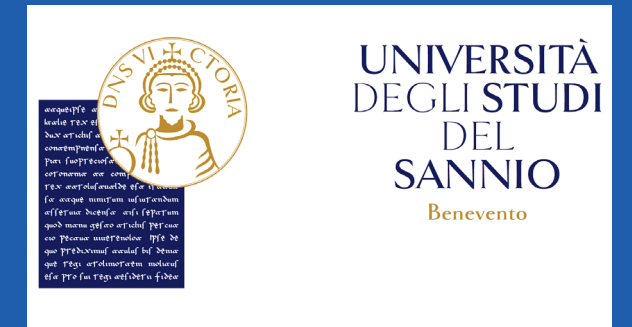
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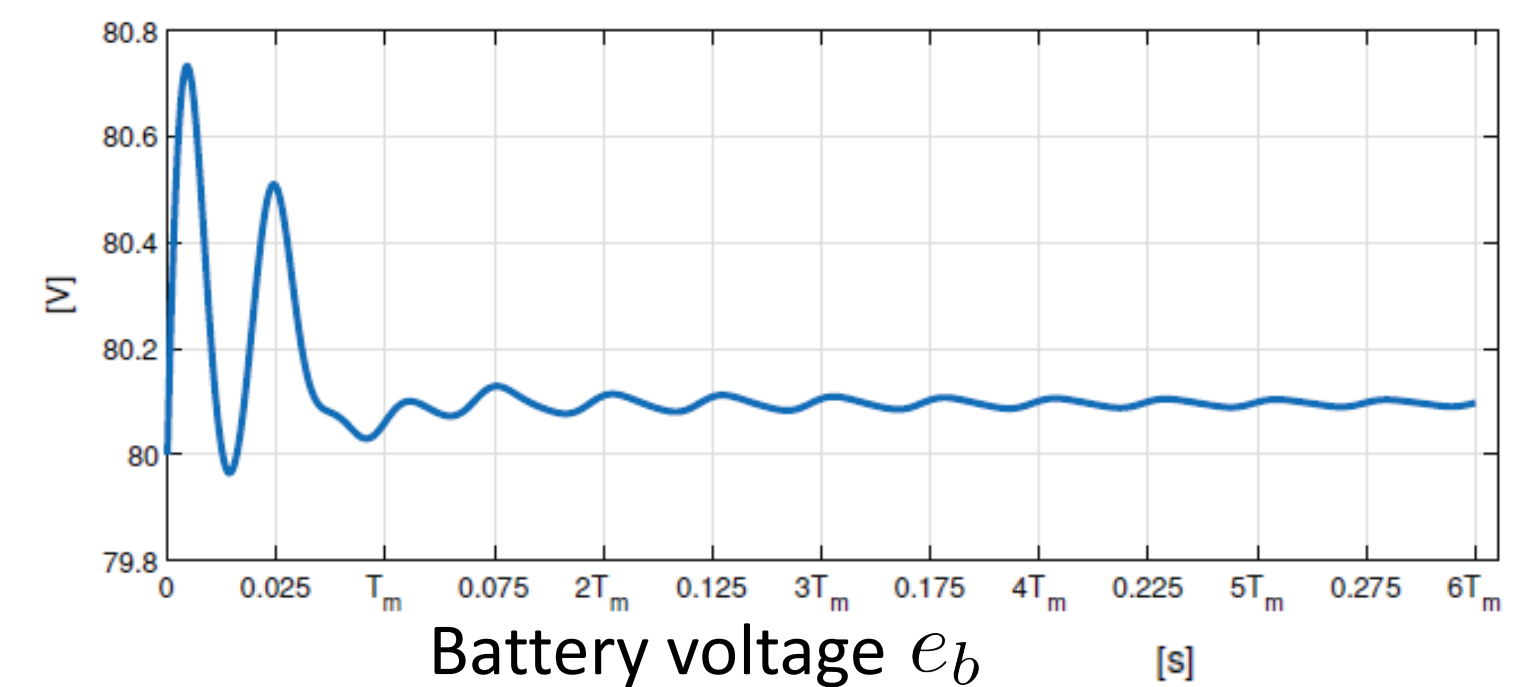
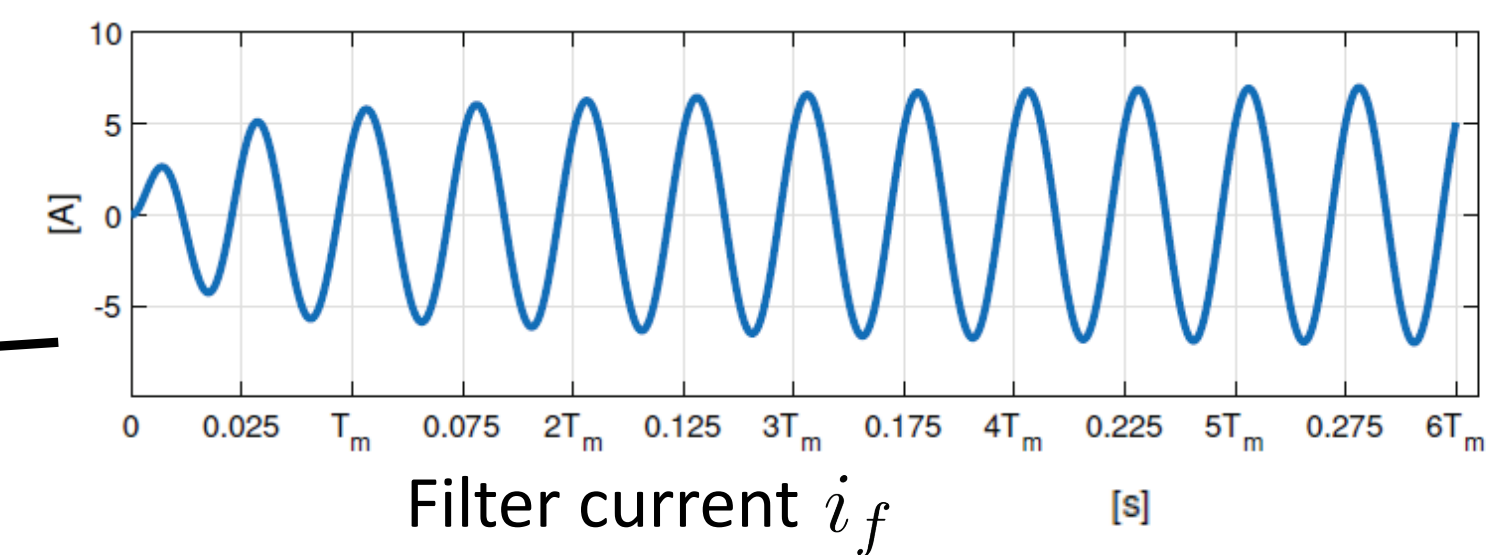
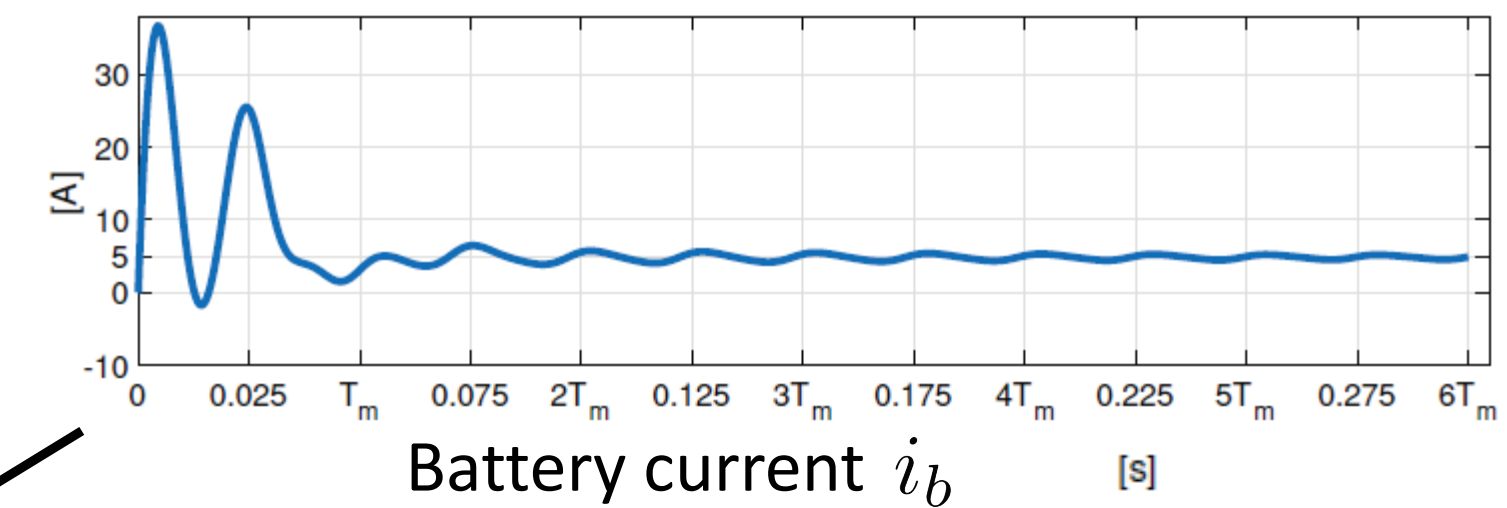
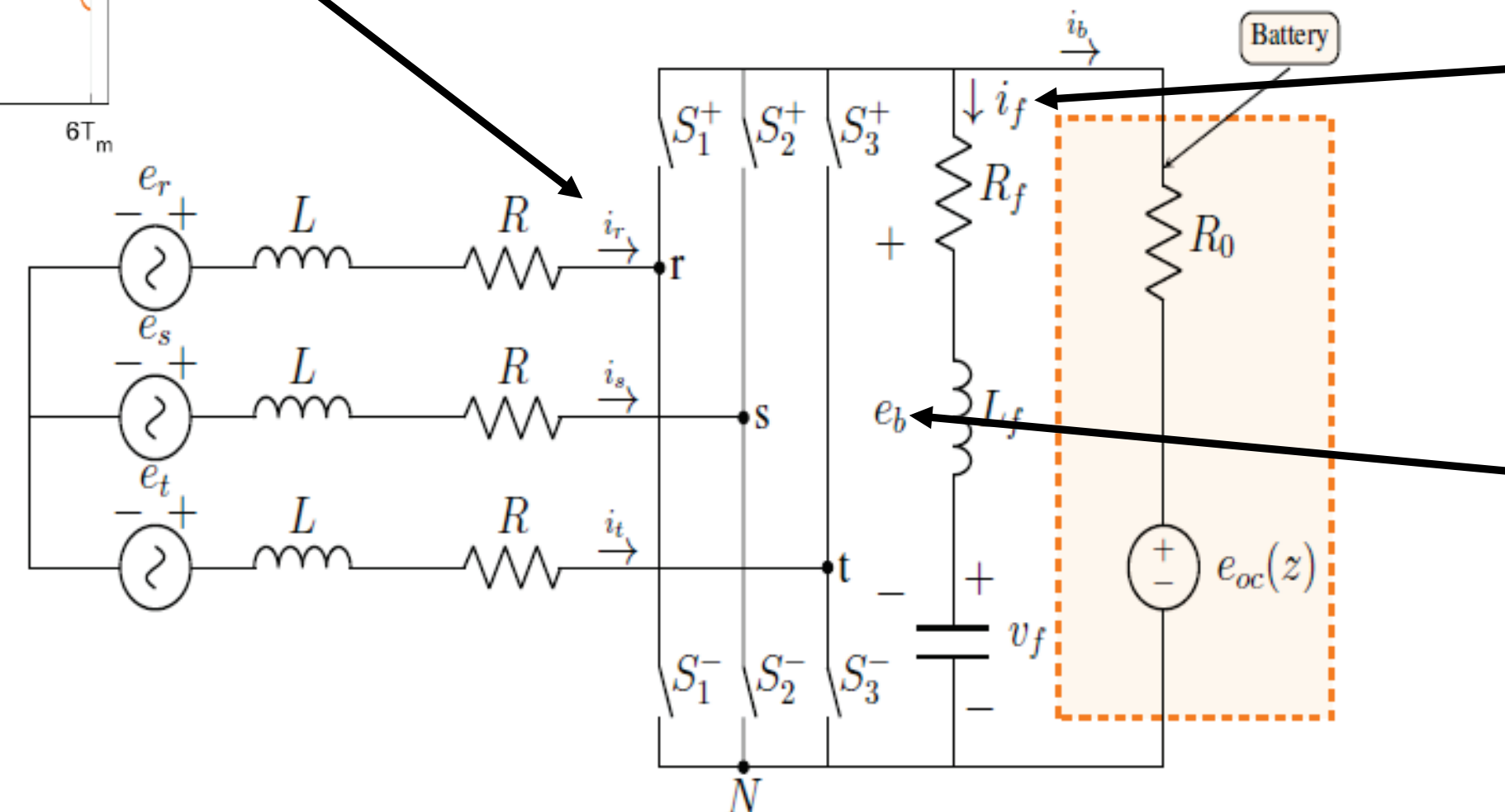
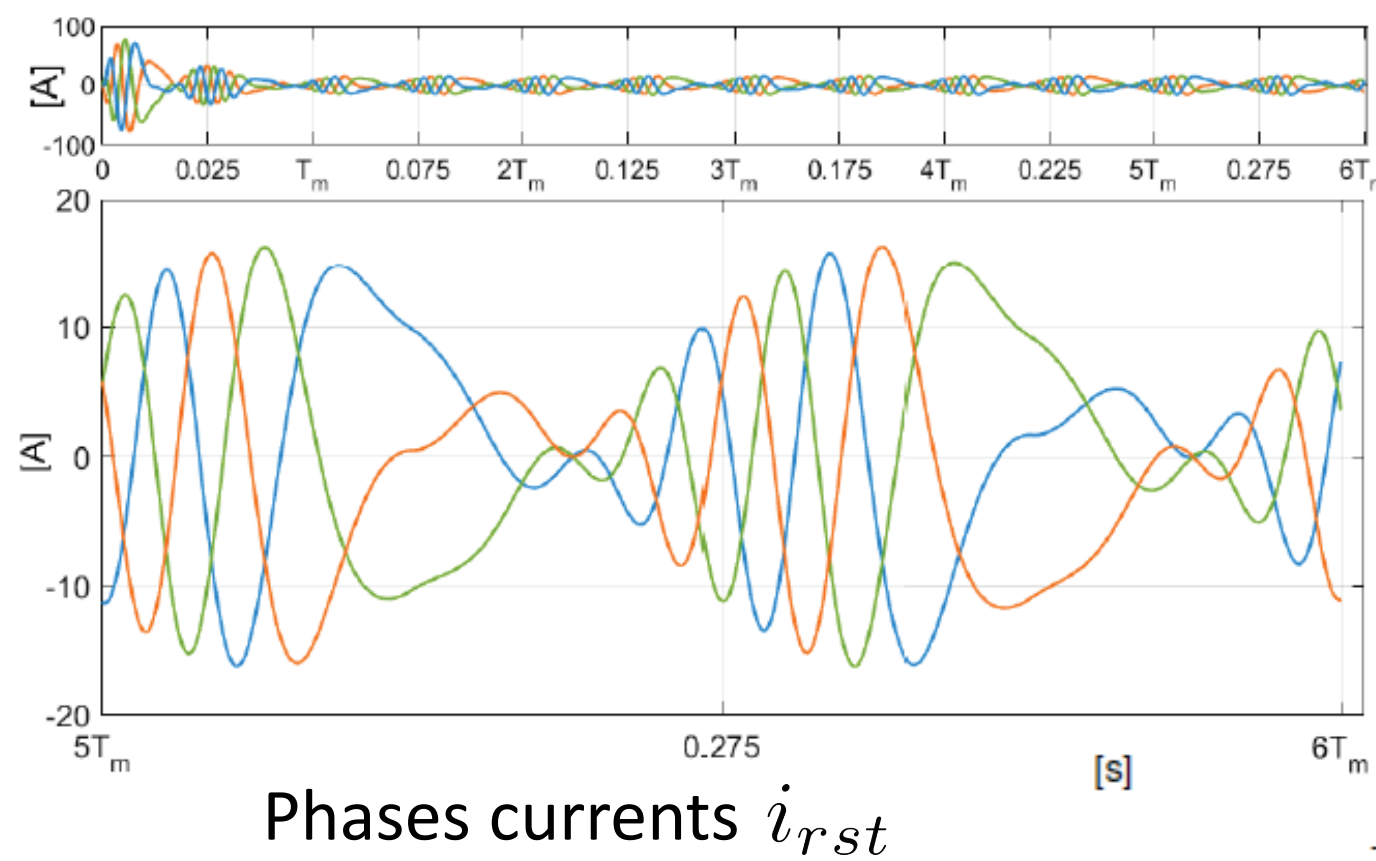


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Control – numerical analysis

- A digital twin of the FLPG + Battery + Control has been developed in Matlab/Simulink



Polyphase FPLG design

- Within the Free-Most a polyphase FPLG is under design



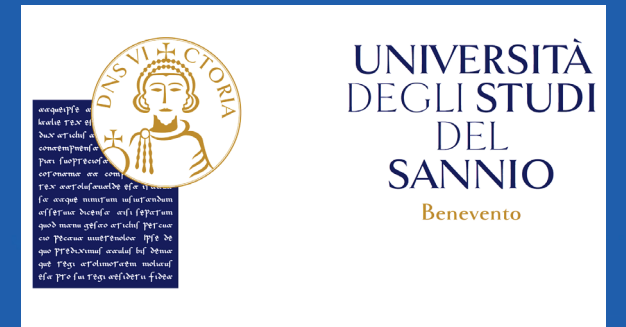
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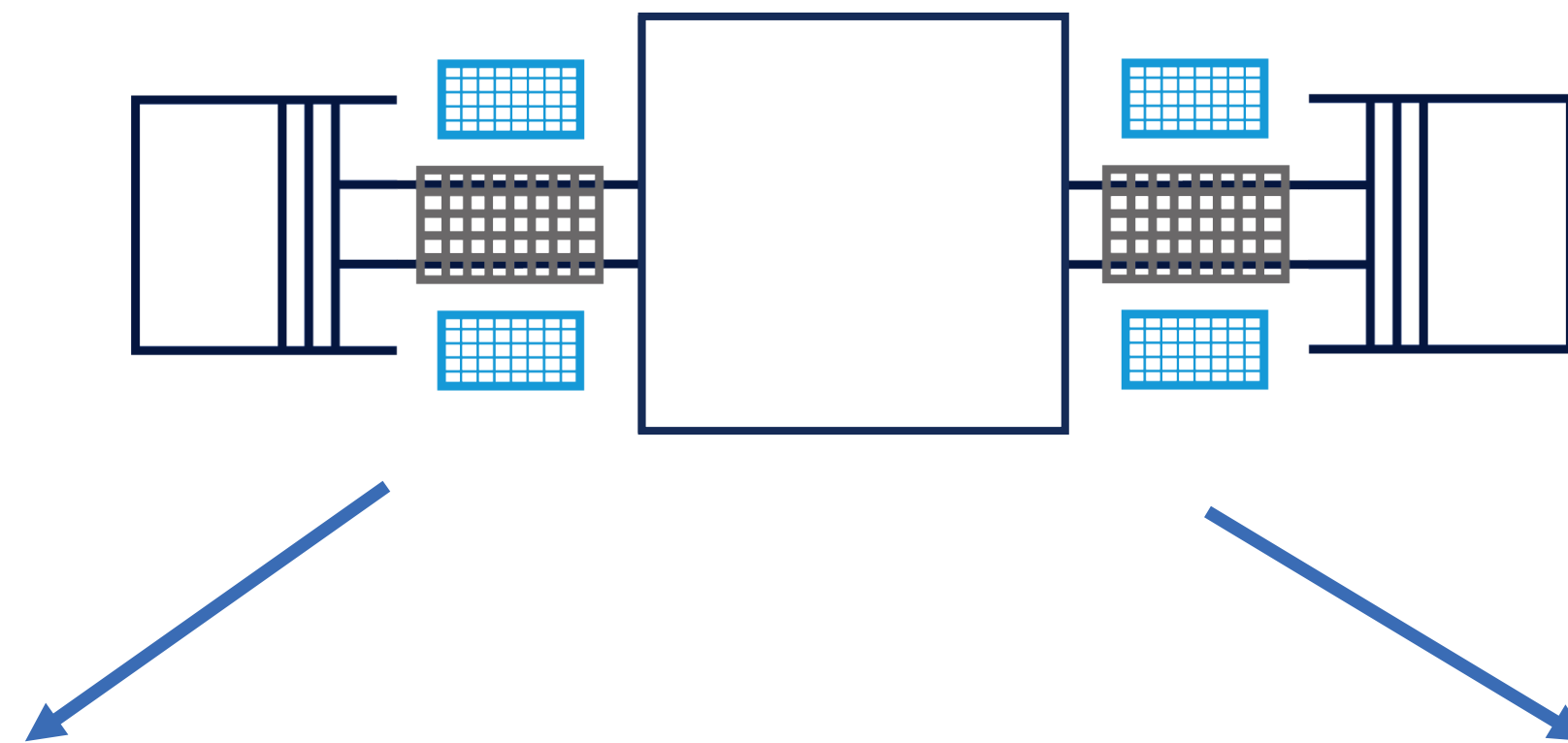


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Test rig

- Procurement of the test rig is started and the test rig is under development



- A linear motor is used as motor and controlled in position/velocity
- It emulates the gas expansion

- The second linear motor is used as generator to test the developed controller

- Single linear motor data:
 - 5kW
 - Frequency 5Hz
 - Travel length (one-way): 250 mm
 - Mass: 10 kg
 - Average velocity: 2.45 m/s



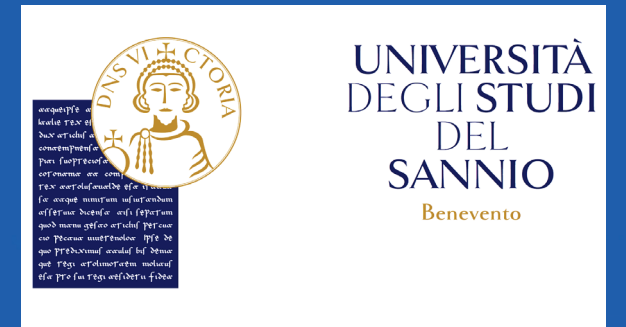
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Conclusions

- Achievements:
 - Model of the FPLG + Converter + Battery
 - Design of the controller for battery recharging
 - Digital twin development and validation
 - Design of a polyphase linear motor
 - Test rig design and procurement
- Publications:
 - A conference paper accepted
 - A conference paper submitted
- Dissemination:
 - A conference
 - A workshop

Future works

- Increase the power size and the frequency of the test rig
- Modify the developed controller for piston-like expansion motion
- Derive a control system for the piston position
- Extend the control to a polyphase motor
- Evaluate the possibility to consider a supercapacitor in the electrical scheme
- Emulate the combustion through compressed air
- Include combustion